
FNCE 926

Empirical Methods in CF

Lecture 7 – Natural Experiment [P2]

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Announcements & Informal Survey

- Exercise #3 is due
- Please fill out informal survey
 - Helps me figure out what changes I can make to improve the course for the second half and for future years
 - For example, what topic should I have spent more time on? What topic did you find the most interesting? Is there too much, or too little work? Etc.

Background readings

- Roberts and Whited
 - *Sections 2.2, 4*
- Angrist and Pischke
 - *Section 5.2*

Outline for Today

- Quick review of last lecture
- Continue to discuss natural experiments
 - How to handle multiple events
 - Triple differences
 - Common robustness tests that can be used to test whether internal validity is likely to hold
- Student presentations of “NE #1” papers

Quick Review *[Part 1]*

- Natural experiment provides random variation in x that allows causal inference
 - Can be used in IV, regression discontinuity, but most often associated with “treatment” effects
- Two types of simple differences
 - Post-treatment comparison of treated & untreated
 - Pre- and post-treatment comparison of treated

Quick Review [Part 2]

- Difference-in-differences is estimated with...

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + u_{i,t}$$

- Compares change in y pre- versus post-treatment for treated to change in y for untreated
 - Requires “parallel trends” assumption
- Let’s test your ability to identify a violation of the necessary assumptions for simple diffs and diff-in-diffs...

Quick Review *[Part 3]*

- Suppose Spain exits the Euro. And, Ann compares profitability of Spanish firms after the exit to profitability before...
- **What is necessary for the comparison to have any causal interpretation?**
 - **Answer =** We must assume profitability after Spain's exit would have been same as profitability prior to exit absent exit... Highly implausible

Quick Review *[Part 4]*

- Now, suppose Bob compares profitability of Spanish firms after the exit to profitability of German firms after exit...
- **What is necessary for the comparison to have any causal interpretation?**
 - **Answer** = We must assume profitability of Spanish firm would have been same as profitability of German firms absent exit...
Again, this is highly implausible

Quick Review *[Part 5]*

- Lastly, suppose Charlie compares change in profitability of Spanish firms after exit to change in profitability of German firms
- **What is necessary for the comparison to have any causal interpretation?**
 - **Answer** = We must assume change in profitability of Spanish firm would have been same as change for German firms absent exit... I.e. parallel trends assumption

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
 - Using group means to get an estimate
 - When additional controls are appropriate
- How to handle multiple events
- Falsification tests
- Triple differences

Standard Regression Format

- Difference-in-differences estimator

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + u_{i,t}$$

- $p_t = 1$ if period t occurs after treatment and equals zero otherwise
- $d_i = 1$ if unit is in treated group and equals zero otherwise

But, there is another way that just involves comparing four sample means...

Comparing group means approach

- To see how we can get the same estimate, β_3 , by just comparing sample means, first calculate expected y under four possible combinations of p and d indicators

Comparing group means approach [P1]

- Again, the regression is...

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + u_{i,t}$$

- And, the four possible combinations are:

$$E(y | d = 1, p = 1) = \beta_0 + \beta_1 + \beta_2 + \beta_3$$

$$E(y | d = 1, p = 0) = \beta_0 + \beta_2$$

$$E(y | d = 0, p = 1) = \beta_0 + \beta_1$$

$$E(y | d = 0, p = 0) = \beta_0$$

What assumption did I
make in doing this?

←
Answer: $E(u | d, p) = 0$; i.e.
the “experiment” is random

Comparing group means approach [P2]

$$E(y | d = 1, p = 1) = \beta_0 + \beta_1 + \beta_2 + \beta_3$$

$$E(y | d = 1, p = 0) = \beta_0 + \beta_2$$

$$E(y | d = 0, p = 1) = \beta_0 + \beta_1$$

$$E(y | d = 0, p = 0) = \beta_0$$

- These can be arranged in two-by-two table

	Post-Treatment, (1)	Pre-Treatment, (2)
Treatment, (a)	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$
Control, (b)	$\beta_0 + \beta_1$	β_0

Comparing group means approach [P3]

- Now take the simple differences

	Post-Treatment, (1)	Pre-Treatment, (2)	Difference, (1)-(2)
Treatment, (a)	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$	$\beta_1 + \beta_3$
Control, (b)	$\beta_0 + \beta_1$	β_0	β_1
Difference, (a)-(b)	$\beta_2 + \beta_3$	β_2	

Comparing group means approach [P4]

- Then, take difference-in-differences!

	Post-Treatment, (1)	Pre-Treatment, (2)	Difference, (1)-(2)
Treatment, (a)	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$	$\beta_1 + \beta_3$
Control, (b)	$\beta_0 + \beta_1$	β_0	β_1
Difference, (a)-(b)	$\beta_2 + \beta_3$	β_2	β_3

This is why they call it the difference-in-differences estimate; regression gives you same estimate as if you took differences in the group averages

Simple difference – Revisited [Part 1]

- Useful to look at simple differences

	Post-Treatment, (1)	Pre-Treatment, (2)	Difference, (1)-(2)
Treatment, (a)	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$	$\beta_1 + \beta_3$
Control, (b)	$\beta_0 + \beta_1$	β_0	β_1
Difference, (a)-(b)	$\beta_2 + \beta_3$	β_2	β_3

↑
This was cross-sectional
simple difference

When does that simple diff
give effect of treatment, β_3 ?

Answer = when β_2 equals
zero; i.e. no difference in level
of y absent treatment

Simple difference – Revisited [Part 2]

- Now, look at time-series simple diff...

	Post-Treatment, (1)	Pre-Treatment, (2)	Difference, (1)-(2)
Treatment, (a)	$\beta_0 + \beta_1 + \beta_2 + \beta_3$	$\beta_0 + \beta_2$	$\beta_1 + \beta_3$
Control, (b)	$\beta_0 + \beta_1$	β_0	β_1
Difference, (a)-(b)	$\beta_2 + \beta_3$	β_2	β_3

This was time-series
simple difference

When does that simple diff
give effect of treatment, β_3 ?

Answer = when β_1 equals zero; i.e.
no change in y absent treatment

Why the regression is helpful

- Some papers will just report this simple two-by-two table as their estimate
- But, there are advantages to the regression
 - Can modify it to test timing of treatment
[we will talk about this in robustness section]
 - Can add additional controls, X

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
 - Using group means to get an estimate
 - When additional controls are appropriate
- How to handle multiple events
- Falsification tests
- Triple differences

Adding controls to diff-in-diff

- Easy to add controls to regression

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + \Gamma X_{i,t} + u_{i,t}$$

- X is some vector of controls
 - Γ is vector of coefficients
- $E[y | d, p]$ in prior proofs just becomes $E[y | d, p, X]$

**From earlier lecture,
what type of controls
should you NEVER add?**

When controls are inappropriate

- Remember! You should never add controls that might themselves be affected by treatment
 - Angrist-Pischke call this a “bad control”
 - You won’t be able to get a consistent estimate of β_3 from estimating the equation

A Pet Peeve of TG – *Refined*

- If you have a treatment that is truly random, do not put in controls affected by the treatment!
 - I've had many referees force me to add controls that are likely to be affected by the treatment...
 - If this happens to you, put in both regressions (with and without controls), and at a minimum, add a caveat as to why adding controls is inappropriate

When controls are appropriate

- Two main reasons to add controls
 - Improve precision (i.e. lower standard errors)
 - Restore 'random' assignment of treatment

#1 – To improve precision

- Adding controls can soak up some of residual variation (i.e. noise) allowing you to better isolate the treatment effect
 - Should the controls change the estimate?
 - NO! If treatment is truly random, adding controls shouldn't affect actual estimate; they should only help lower the standard errors!
 - If adding controls changes estimates, you might have 'bad controls' *or* worse, non-random treatment ☹

Example – Improving precision

- Suppose you have firm-level panel data
- Some natural experiment ‘treats’ some firms but not other firms
 - Could just estimate the standard diff-in-diff

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + u_{i,t}$$

- *Or*, could add fixed effects (like firm and year FE) to get more precise estimate...

Example – Improving precision [Part 2]

- So, suppose you estimate...

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 (d_i \times p_t) + \alpha_i + \delta_t + u_{i,t}$$

Firm fixed effects

Year fixed effects

- What meaning does β_1 have now?
- What meaning does β_2 have now?

Example – Improving precision [Part 3]

- Trick question! They have no meaning!
 - p_t is perfectly collinear with year FE
[because it doesn't vary across firms]
 - d_i is perfectly collinear with firm FE
[because it doesn't vary across time for each firm]
- Stata just randomly drops a couple of the FE
 - The estimates on p_t and d_i are just random intercepts with **no** meaning

Example – Improving precision [Part 4]

- Instead, you should estimate...

$$y_{i,t} = \beta_0 + \beta_3 (d_i \times p_t) + \alpha_i + \delta_t + u_{i,t}$$

Firm fixed effects
control for treatment

Year fixed effects
control for post-
treatment

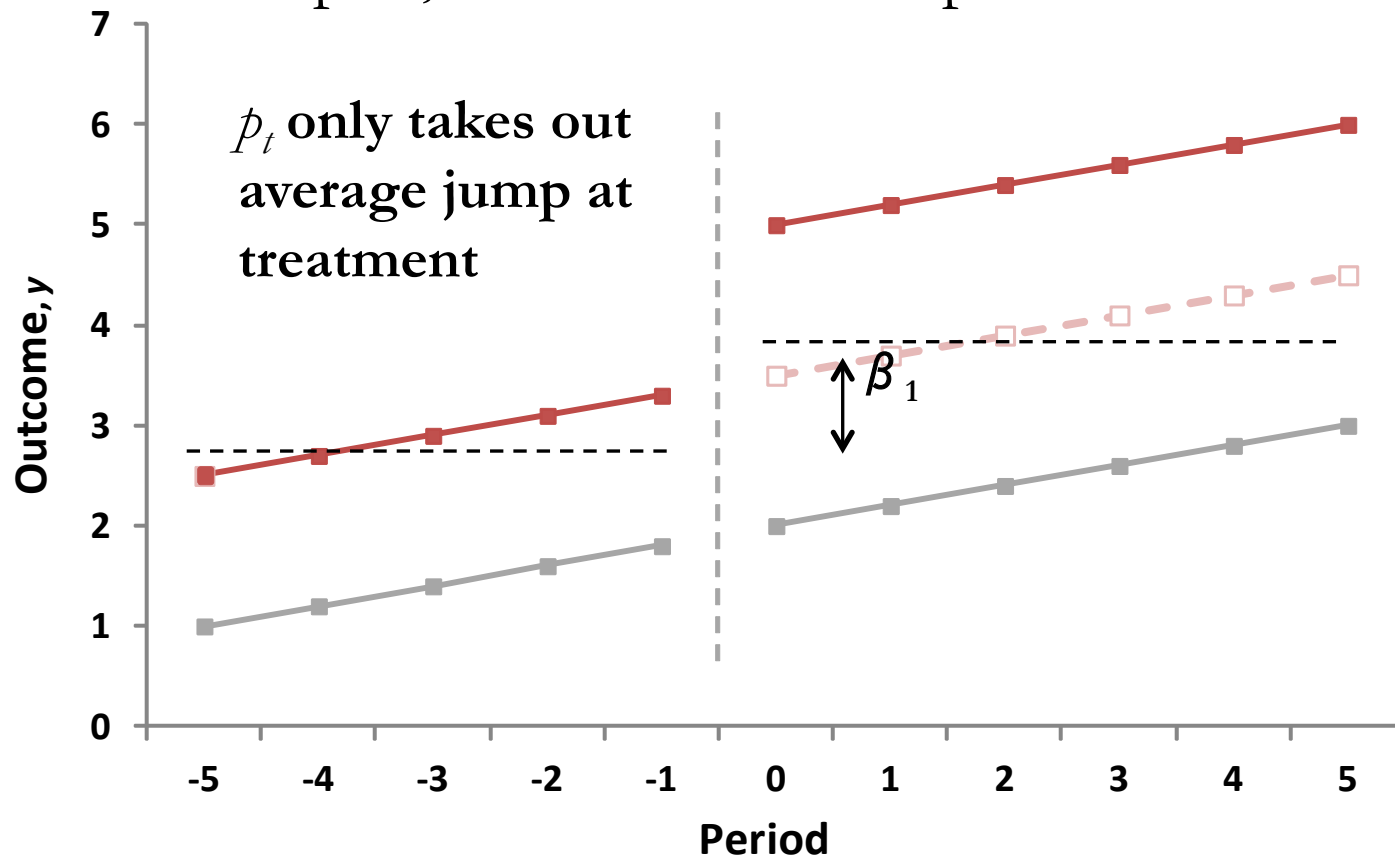
- **This is what some call the generalized difference-in-differences estimator**

Generalized Difference-in-differences

- Advantage of generalized differences-in-differences is that it can improve precision and provide better fit of model
 - It doesn't assume all firms in treatment (or untreated) group have same average y ; it allows intercept to vary for each firm
 - It doesn't assume that common change in y around event is a simple change in level; it allows common change in y to vary by year

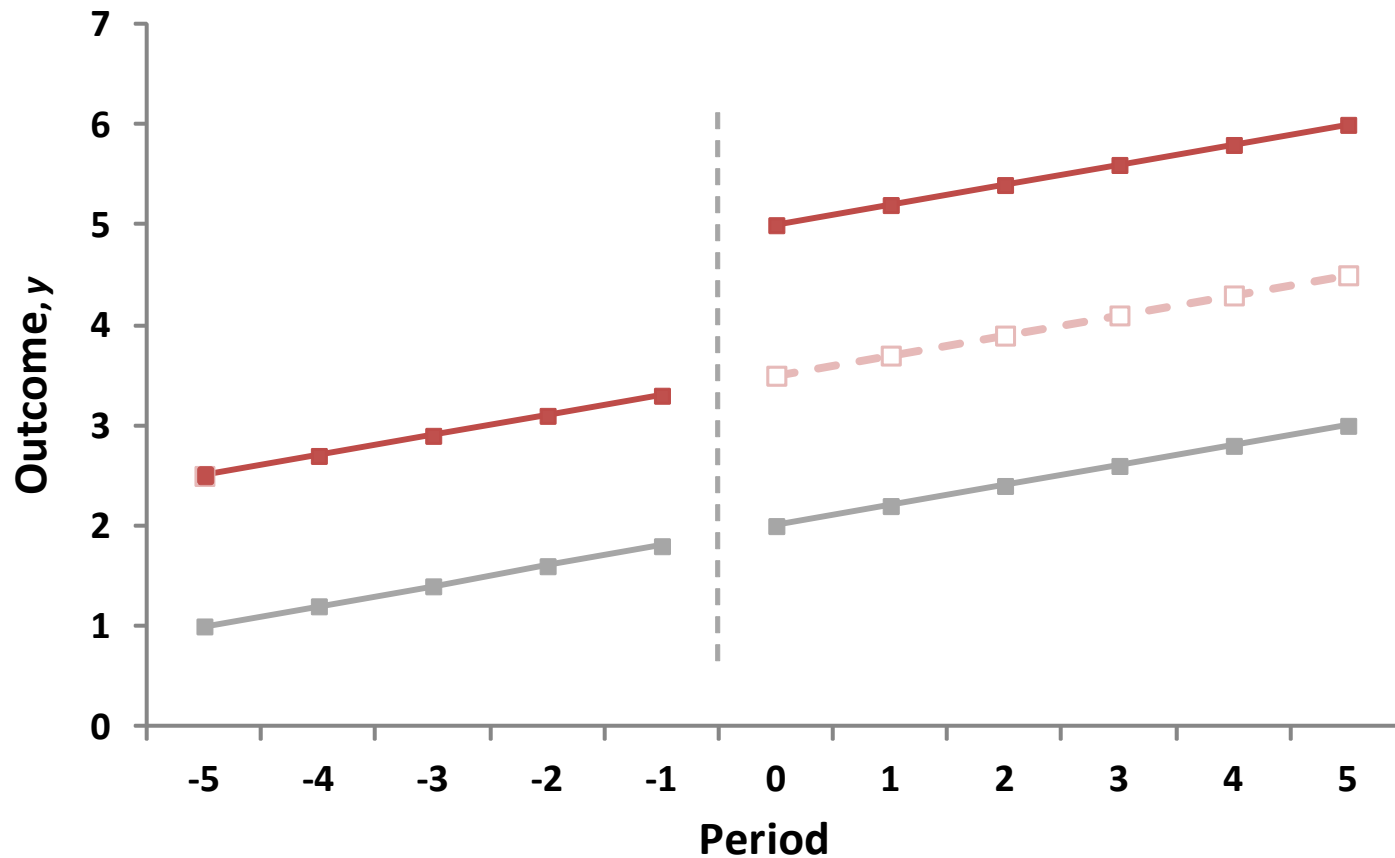
Generalized D-i-D – Example [Part 1]

- To see how Generalized D-i-D can be helpful, consider the example from last week



Generalized D-i-D – *Example [Part 2]*

- Year dummies will better fit actual trend



When controls are appropriate

- Two main reasons to add controls
 - Improve precision (i.e. lower standard errors)
 - Restore 'random' assignment of treatment

#2 – Restore randomness of treatment

- Suppose the following is true...
 - Observations of certain characteristic, e.g. high x , are more likely to be treated
 - **And**, firms with this characteristic are likely to have differential trend in outcome y
 - Adding control for x could restore ‘randomness’; i.e. being treated is random after controlling for x !
- I.e. treatment isn’t random
- And, non-randomness is problematic for identification

Restoring randomness – *Example*

- Natural experiment is change in regulation
 - Firms affected by regulation is random, except that it is more likely to hit firms that are larger
 - *And*, we think larger firms might have different trend in outcome y afterwards for other reasons
 - *And*, firm size is not going to be affected by the change in regulation in any way
- If all true, adding size as control would be an appropriate and desirable thing to do

Controls continued...

- In prior example, suppose size is potentially effected by the change in regulation...
- What would be another approach that won't run afoul of the 'bad control' problem?
 - **Answer:** Use firm size in year prior to treatment and it's interaction with post-treatment dummy
 - This will control for non-random assignment (based on size) and differential trend (based on size)

Restoring randomness – Caution!

- In practice, don't often see use of controls to restore randomness
 - Requires assumption that non-random assignment isn't also correlated with unobservable variables...
 - So, not that plausible unless there are very specific reasons for non-randomness
- **But, regression discontinuity is one example of this; we'll see it next week**

One last note... be careful about SEs

- Again, if have multiple pre- and post-treatment periods, need to be careful with standard errors
 - Either cluster SEs at level of each unit
 - Or, collapse data down to one pre- and one post-treatment observation for each cross-section
- We will discuss more about standard errors in lecture on “standard errors”

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
- How to handle multiple events
 - Why they are useful
 - Two similar estimation approaches
- Falsification tests
- Triple differences

Motivating example...

- Gormley and Matsa (2011) looked at firms' responses to increased left-tail risk
 - Used discovery that workers were exposed to harmful chemical as exogenous increase in risk
 - One discovery occurred in 2000; a chemical heavily used by firms producing semiconductors was found to be harmful
- Can you think of any concerns about parallel trends assumption of this setting?

Motivating Example – *Answer*

- **Answer:** Yes... This coincides with bursting of technology bubble; technology firms might arguably trend differently after 2000 for this reasons unrelated to chemical
- How might multiple treatment events, occurring at different times (which is what Gormley and Matsa used), help?

Multiple treatment events

- Sometimes, the natural experiment is repeated a multiple points in times for multiple groups of observations
 - E.g. U.S. states make a particular regulatory change at different points in time
- **These settings are particularly useful in mitigating concerns about violation of parallel trends assumption...**

How multiple events are helpful

- Can show that effect of treatment is similar across different time periods
- Can show effect of treatment isn't driven by a particular set of treated firms
 - I.e. now the “identification police” would need to come up with story as to why parallel trends is violated for each unique event

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
- How to handle multiple events
 - Why they are useful
 - Two similar estimation approaches
- Falsification tests
- Triple differences

Estimation with Multiple Events

- Estimating model with multiple events is still relatively easy to do
 - Use approach of Bertrand and Mullainathan (JPE 2003)
 - Or, used “stacked” approach of Gormley and Matsa (RFS 2011)

Multiple Events – Approach #1 [P1]

- Just estimate the following estimation

$$y_{ict} = \beta d_{ict} + p_t + m_c + u_{ict}$$

- y_{ict} is outcome for unit i (e.g. firm) in period t (e.g. year) and cohort c , where “cohort” indexes the different sets of firms treated by each event
 - E.g. different firms might be affected by a change in regulation at different points in time; firms **affected** at one point in time are a ‘cohort’

Multiple Events – Approach #1 [P2]

$$y_{ict} = \beta d_{ict} + p_t + m_c + u_{ict}$$

d_{ict} = indicator on whether cohort c is affected by time t ; this is the interaction between *treatment* & *post*

Time period fixed effects; they will control for *post* dummy in each event

Cohort fixed effects; they are the control for the *treatment* dummy in each event

Multiple Events – Approach #1 [P3]

- Intuition of this approach...
 - Every untreated observation at a particular point in time acts as control for treated observations in that time period
 - E.g. a firm treated in 1999 by some event will act as a control for a firm treated in 1994 until itself becomes treated in 1999
 - β will capture average treatment effect across the multiple events

Multiple Events – Approach #2 [P1]

- Now, think of running generalized diff-in-diff for just one of the multiple events...

$$y_{it} = \beta(d_i \times p_t) + \alpha_i + \delta_t + u_{it}$$

- d_i = indicator for unit i (e.g. firm) being a treated firm in that particular event
- p_t = indicator for treatment having occurred by period t (e.g. year)
- Unit i and period t FE control for the independent effects of d_i and p_t

Multiple Events – Approach #2 [P2]

- But, contrary to standard difference-in-difference, your sample is...
 - Restricted to a small window around event; e.g. 5 years pre- and post- event
 - And, drops any observations that are treated by another event
 - I.e. your sample starts only with previously untreated observations, and if a ‘control’ observation later gets treated by a different event, those post-event observations are dropped

Multiple Events – Approach #2 [P3]

- Now, create a similar sample for each “event” being analyzed
- Then, “stack” the samples into one dataset and create a variable that identifies the event (i.e. ‘cohort’) each observation belongs to
 - **Note:** some observation units will appear multiple times in the data [e.g. firm 123 might be a control in event year 1999 but a treated firm in a later event in 2005]

Multiple Events – Approach #2 [P4]

- Then, estimate the following on the stacked dataset you've created

$$y_{ict} = \beta d_{ict} + \delta_{tc} + \alpha_{ic} + u_{ict}$$

d_{ict} = indicator on whether cohort c is affected by time t ; this is the interaction between *treatment* & *post*

Time-cohort period fixed effects;
they control for *post* dummy in each event (i.e. for each 'stack')

Unit-cohort FE;
they control for the *treatment* dummy in each cohort (i.e. in each 'stack')

Multiple Events – Approach #2 [P5]

- This approach has same intuition of the first approach, but has a couple advantages
 - Can more easily isolate a particular window of interest around each event
 - Prior approach compared all pre- versus post-treatment observations against each other
 - Can more easily extend this into a triple-difference type specification [*more on that later*]

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
- How to handle multiple events
- Falsification tests
- Triple differences

Falsification Tests for D-i-D

- Can never directly test underlying identification assumption, but can do some falsification tests to support its validity
 - #1 – Compare pre-treatment observables
 - #2 – Check that timing of observed change in y coincides with timing of event [*i.e. no pre-trend*]
 - #3 – Check for treatment reversal
 - #4 – Check variables that shouldn't be affected
 - #5 – Add a triple-difference

#1 – Pre-treatment comparison *[Part 1]*

- Idea is that experiment ‘randomly’ treats some subset of observations
 - If true, then ex-ante characteristics of ‘treated’ observations should be similar to ex-ante characteristics of ‘untreated’ observations
 - Showing treated and untreated observations are comparable in dimensions thought to affect y can help ensure assignment was random

#1 – Pre-treatment comparison *[Part 2]*

- If find ex-ante difference in some variable z , is difference-in-difference is invalid?
 - **Answer** = Not necessarily.
 - We need some story as to why units are expected to have differential trend in y after treatment (for reasons unrelated to treatment) that is correlated with z for this to actually be a problem for identification
 - **And**, even with this story, we could just control for z and it's interaction with time
 - **But, what would be the lingering concern?**

#1 – Pre-treatment comparison *[Part 3]*

- **Answer = unobservables!**
 - If the treated and control differ ex-ante in observable ways, we worry they might differ in unobservable ways that related to some violation of the parallel trends assumption

#2 – Check for pre-trend [*Part 1*]

- Similar to last lecture, can just allow effect of treatment to vary by period to non-parametrically map out the timing
 - “Parallel trends” suggest we shouldn’t observe any differential trend prior to treatment for the observations that are eventually treated

#2 – Check for pre-trend [Part 2]

- Estimate the following:

$$y_{i,t} = \beta_0 + \beta_1 d_i + \beta_2 p_t + \sum_t \gamma_t (d_i \times \lambda_t) + u_{i,t}$$

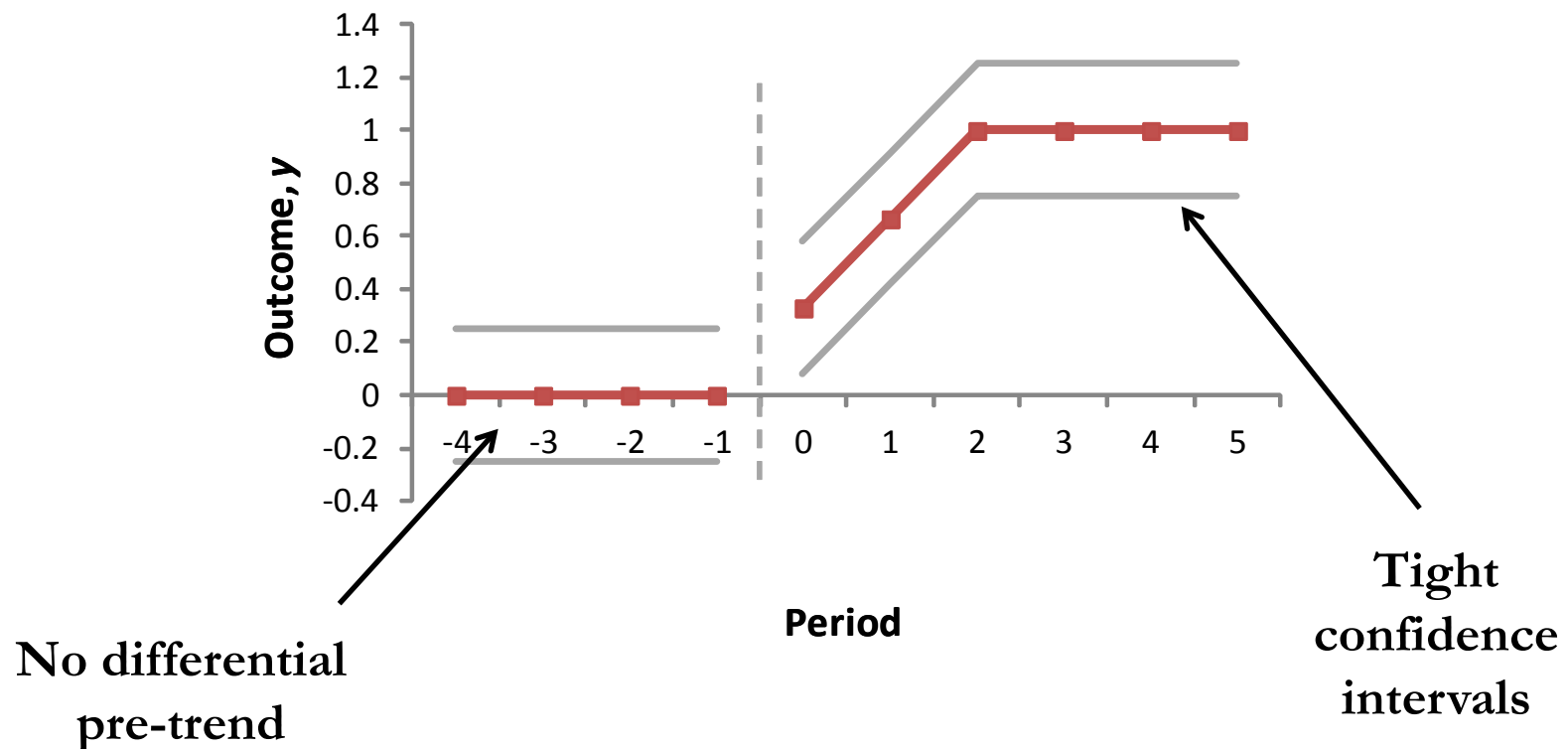
- d_i and p_t are defined just as before
- λ_t is indicator that equals 1 if event time = t and zero otherwise, where
 - $t = 0$ is the period treatment occurs
 - $t = -1$ is period before treatment

#2 – Check for pre-trend [*Part 3*]

- Υ_t estimates change in y relative to excluded periods; you then plot these in graph
 - Easiest to **fully saturate** the model (i.e. include λ_t for every period but the very first one); then all estimates Υ_t are relative to this period
 - Can also plot confidence interval for each Υ_t

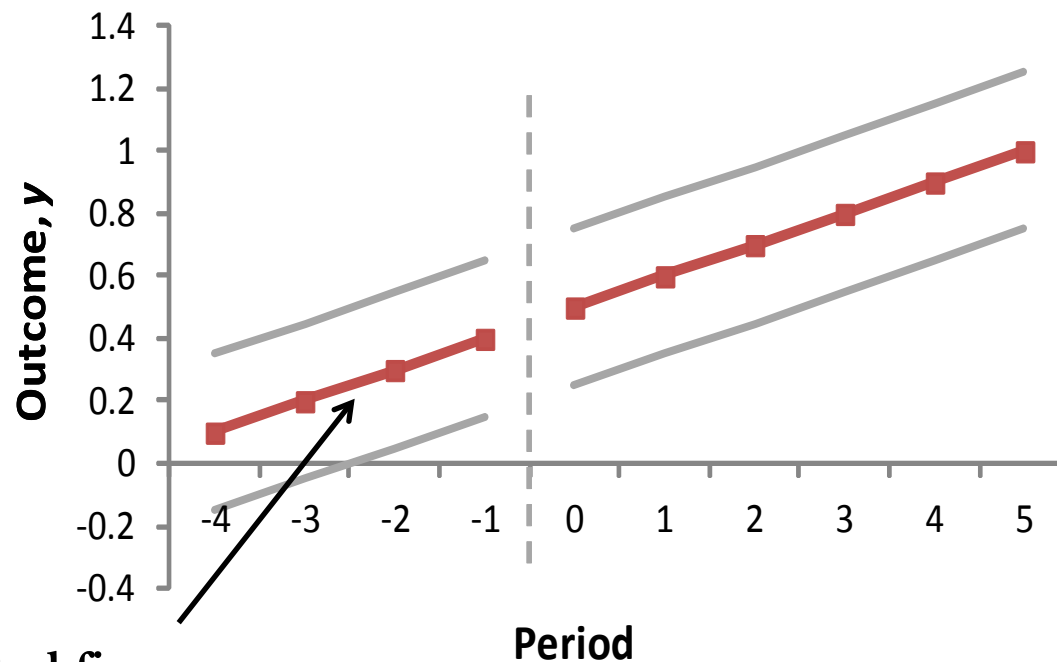
#2 – Check for pre-trend [Part 4]

- Something like this is ideal...



#2 – Check for pre-trend [Part 5]

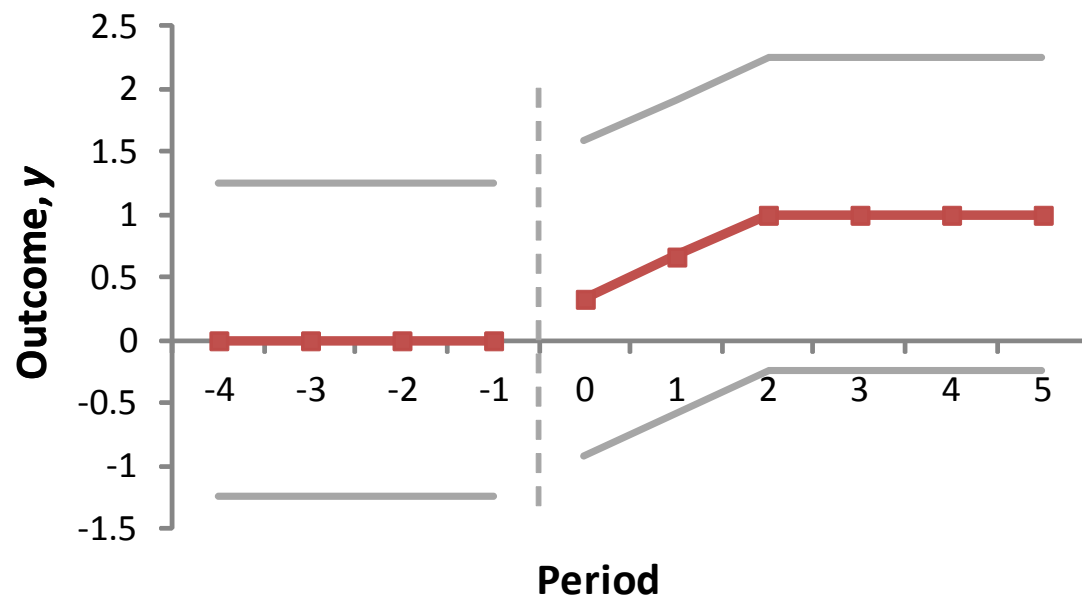
- Something like this is very bad



y for treated firms was
already going up at faster
rate prior to event!

#2 – Check for pre-trend [Part 6]

- Should we make much of wide confidence intervals in these graphs? E.g.



Answer: Not too much... Each period point estimate might be noisy; diff-in-diff will tell us whether post-average y is significantly different then pre-average y

#2 – Check for pre-trend [*Part 7*]

- Another type of pre-trend check done is to do the diff-in-diff in some “random” pre-treatment to show no effect
 - I’m not a big fan of this... Why?
 - **Answer #1** – It is subject to gaming; researcher might choose a particular pre-period to look at that works
 - **Answer #2** – Prior approach allows us to see what the timing was and determine whether it is plausible

#3 – Treatment reversal

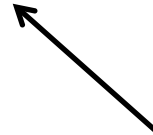
- In some cases, the “natural experiment” is subsequently reversed
 - E.g. regulation is subsequently undone
- If we expect the reversal should have the opposite effect, it is good to confirm this

#4 – Unaffected variables

- In some cases, theory provides guidance on what variables should be unaffected by the “natural experiment”
 - If natural experiment is what we think it is, we should see this in the data... so check

#5 – Add Triple difference

- If theory tells us treatment effect should be larger for one subset of observations, we can check this with triple difference
 - Pre- *versus* post-treatment
 - Untreated *versus* treated
 - Less sensitive *versus* More sensitive



**This is the third
difference**

Natural Experiment Outline – *Part 2*

- Difference-in-difference continued...
- How to handle multiple events
- Falsification tests
- Triple differences
 - How to estimate & interpret it
 - Using the popular subsample approach

Diff-in-diff-in-diff – Regression

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 h_i + \beta_4 (p_t \times h_i) \\ + \beta_5 (d_i \times h_i) + \beta_6 (p_t \times d_i) + \beta_7 (p_t \times d_i \times h_i) + u_{i,t}$$

- $p_t = 1$ if period t occurs after treatment and equals zero otherwise
- $d_i = 1$ if unit is in treated group and equals zero otherwise
- $h_i = 1$ if unit is group that is expected to be more sensitive to treatment

Diff-in-diff-in-diff – Regression *[Part 2]*

- How to choose and set b_i
 - E.g. If theory says effect is bigger for larger firms; could set $b_i = 1$ if assets of firm in year prior to treatment is above the median size
 - **Note:** Remember to use ex-ante measures to construct indicator if you think underlying variable (that determines sensitivity) might be affected by treatment... Why?
 - **Answer =** To avoid bad controls!

Diff-in-diff-in-diff – Regression [Part 3]

$$y_{i,t} = \beta_0 + \beta_1 p_t + \beta_2 d_i + \beta_3 h_i + \beta_4 (p_t \times h_i) \\ + \beta_5 (d_i \times h_i) + \beta_6 (p_t \times d_i) + \beta_7 (p_t \times d_i \times h_i) + u_{i,t}$$

- Easy way to check if done correctly...
 - Should have 8 coefficients (including constant) to capture the $2 \times 2 \times 2 = 8$ different combinations
 - Likewise, a double difference has 4 coefficients (including constant) for the $2 \times 2 = 4$ combinations
- What do β_6 and β_7 capture?

Interpreting the estimates [*Part 1*]

- β_6 diff-in-diff estimate for the less-sensitive obs.
 - Captures average differential change in y from the pre- to post-treatment period for the less sensitive observations in the treatment group *relative* to the change in y for the less sensitive observations in the untreated group

Interpreting the estimates *[Part 2]*

- β_7 is the triple diff estimate; it tells us how much larger effect is for the more sensitive obs.
 - β_7 captures how different the difference-in-difference estimate is for observations considered more sensitive to the treatment
 - **What is total treatment effect for these firms?**
 - **Answer = $\beta_6 + \beta_7$**

Tangent – Continuous vs. Indicator?

- Can also do the triple difference replacing b_i with a continuous measure instead of indicator
 - E.g. suppose we expect treatment effect is bigger for larger firms; rather than constructing indicator based on ex-ante size, could just use ex-ante size
 - **What are the advantages, disadvantages of this?**

Tangent – Continuous vs. Indicator?

- Advantages
 - Makes better use of variation available in data
 - Provides estimate on magnitude of sensitivity
- Disadvantages
 - Makes linear functional form assumption; indicator imposes less structure on the data
 - More easily influenced by outliers

Generalized Triple-Difference

- Similar to diff-in-diff, can add in FE to soak up the various terms and improve precision
- E.g. in firm-level panel regression with firm and year fixed effects, you'd estimate

$$y_{i,t} = \beta_1 (p_t \times h_i) + \beta_2 (p_t \times d_i) \\ + \beta_3 (p_t \times d_i \times h_i) + \delta_t + \alpha_i + u_{i,t}$$

- The other terms (including the constant) all drop out; they are collinear with the FE

Natural Experiment [P2] – *Outline*

- Difference-in-difference continued...
- How to handle multiple events
- Falsification tests
- Triple differences
 - How to estimate & interpret it
 - Using the popular subsample approach

Subsample Approach

- Instead of doing full-blown triple-difference, you can also just estimate the double-difference in the two separate subsamples
 - Double-difference for low sensitive obs. (i.e. $h_i = 0$)
 - Double-difference for more sensitive obs. (i.e. $h_i = 1$)
- **Note:** the estimates won't directly match the β_2 , $\beta_2 + \beta_3$ effects in prior estimation... **Why?**

Subsample Approach Differences...

- **Answer** = In subsample approach year FE are allowed to differ by sub-sample
 - Therefore, subsample approach is actually controlling for **more** things
 - However, one can easily recover the subsample estimates in one regression (and test the statistical difference) between subsamples by estimating...

Matching Subsample to Combined [P1]

$$y_{i,t} = \beta_2 (p_t \times d_i) + \beta_3 (p_t \times d_i \times h_i) + \delta_t + (\delta_t \times h_i) + \alpha_i + u_{i,t}$$



**Year FE interacted with
sensitivity indicator**

- Just add interaction between year FE and indicator for being more sensitivity...
 - This allows for different year FE for each subsample, which is what happened when we estimated the subsamples in two separate regressions

Matching Subsample to Combined [P2]

- **In prior regression...**
 - β_2 will equal coefficient from diff-in-diff using just the subsample of less sensitive observations
 - $\beta_2 + \beta_3$ will equal coefficient from diff-in-diff using just the subsample of more sensitive observations
 - t-test on β_3 tells you whether effect for more sensitive subsample is statistically different from that of the less sensitive subsample

Triple Diff – Stacked Regression *[Part 1]*

- Another advantage of stacked regression approach to multiple events is ability to more easily incorporate a triple diff
 - Can simply run stacked regression in separate subsamples to create triple-diff or run it in one regression as shown previously

Triple Diff – Stacked Regression *[Part 2]*

- Can't easily do either of these in approach of Bertrand and Mullainathan (2003)
 - Some observations act as both 'control' and 'treated' at different points in sample; not clear how create subsamples in such a setting

External Validity – Final Note

- While randomization ensures internal validity (i.e. causal inferences), external validity might still be an issue
 - Is the experimental setting representative of other settings of interest to researchers?
 - I.e. can we extrapolate the finding to other settings?
 - A careful argument that the setting isn't unique or that the underlying theory (for why you observe what you observe) is likely to apply elsewhere is necessary

Summary of Today *[Part 1]*

- Diff-in-diff & control variables
 - Don't add controls affected by treatment
 - Controls shouldn't affect estimates, but can help improve precision
- Multiple events are helpful in mitigating concerns about parallel trends assumption

Summary of Today *[Part 2]*

- Many falsification tests one should do to help assess internal validity
 - Ex. #1 – Compare ex-ante characteristics
 - Ex. #2 – Check timing of observed effect
- Triple difference is yet another way to check internal validity and mitigate concerns about identification

In First Half of Next Class

- Regression discontinuity
 - What are they?
 - How are they useful?
 - How do we implement them?
- Related readings... see syllabus

Assign papers for next week...

- Gormley and Matsa (RFS 2011)
 - Risk & CEO agency conflicts
- Becker and Stromberg (RFS 2012)
 - Agency conflicts between equity & debt
- Ashwini (JFE 2012)
 - Investor protection laws & corporate policies

Break Time

- Let's take our 10 minute break
- We'll do presentations when we get back